# Monitoring glacier dynamics and structure using dense seismic arrays







#### Florent Gimbert

PhDs, Postdocs: Ugo Nanni, Celeste Labedz (Caltech)

Other collaborators: Philippe Roux (ISTerre, Grenoble), Albanne Lecointre (ISTerre), Victor Tsai (Brown, USA), Timothy Bartholomaus (Univ. Idaho),

### 1 day on the Argentière Glacier, French Alps





### 1 day on the Argentière Glacier, French Alps



### 1 day on the Argentière Glacier, French Alps



### Subglacial hydrology



### Subglacial hydrology



### Subglacial hydrology



Hoffman et al., 2016

What are the physical characteristics of the subglacial hydrology network (spatial organization, pressure, size)?

How do they evolve with time?

### Glacier crevassing



## Which physical mechanism controls crevasse propagation?

How deep are crevasses?

#### Use arrays of sensors for observing spatial and temporal changes

#### The Argentière Glacier (France)



#### The Lemon Creek Glacier (Alaska)



4

# Understanding source properties based on signal characteristics







(e.g. Bartholomaus et al., 2015)

### How can we best exploit signal characteristics in order to retrieve the underlying physics ?

# Understanding source properties based on signal characteristics







Water flow-induced noise (e.g. Bartholomaus et al., 2015)

# How can we best exploit signal characteristics in order to understand and quantify the underlying physics ?

# How can we best exploit signal characteristics in order to understand and quantify the underlying physics ?

As a glaciologist: What physical mechanisms control

- the propagation of crevasses, in particular through depth ?





Van der Veen, 1998; Weiss, 2004; Krug et al., 2014

Astrolabe Glacier, Antarctica

#### How can we best exploit signal characteristics in order to understand and quantify the underlying physics ?

As a glaciologist: What physical mechanisms control

- the propagation of crevasses, in particular through depth ?
- seismic bed sliding, and does it matter for understanding the overall bed friction?



# How can we best exploit signal characteristics in order to understand and quantify the underlying physics ?

As a glaciologist: What physical mechanisms control

- the propagation of crevasses, in particular through depth ?
- seismic bed sliding, and does it matter for understanding the overall bed friction?
- water flow basal pressure and drainage characteristics ?



#### How can we best exploit signal characteristics in order to understand and quantify the underlying physics ?

As a glaciologist: What physical mechanisms control

- the propagation of crevasses, in particular through depth ?
- seismic bed sliding, and does it matter for understanding the overall bed friction?
- water flow basal pressure and drainage characteristics ?

As a seismologist: How can we best use signal characteristics for retrieving and quantifying

- Source physics ?

- Source spatio-temporal dynamics ?

As a seismologist: How can we best use signal characteristics for retrieving and quantifying

- Source physics ?

Crevasse opening \_\_\_\_\_ OK Stick-slip

Water-flow?

- Source spatio-temporal dynamics ?

Crevasse opening Stick-slip

Water-flow

Build up of appropriate physical frameworks

Use of dense seismic arrays



#### The Argentière Glacier (French Alps)



Gimbert et al., SRL, 2021; Nanni et al., PNAS, 2021; Nanni et al., GRL, 2022



#### The Argentière Glacier (French Alps)



Gimbert et al., SRL, 2021; Nanni et al., PNAS, 2021; Nanni et al., GRL, 2022

#### Observed phase field after an icequake





Use sensors as « antennas » The same sources are detected by several sensors, and thus can be located through array phase delay processing

The Argentière Glacier (French Alps)

**100** seismic stations 40-m interspacing ~600 m coverage Measurements 1 month-long records Basal sliding Water discharge Seismic sensors

Gimbert et al., 2021; Nanni et al., 2021; Nanni et al., 2022

Use sensors « independantly » Sensors see distinct enough sources that seismic power at each station pictures local subglacial flow conditions

#### The Lemon Creek Glacier (Alaska)









Matched-field-processing (MFP)

- Consider 1 second-long signals
- Calculate the cross-spectral density matrix as

 $K(\omega) = d(\omega)d^{H}(\omega),$ 

with  $d(\omega)$  the complex data vector and H the Hermitian (conjugate) transpose

• Evaluate the match between the observed and modelled phases in a 4 dimensional space as

$$B_{Bartlett}(\omega_{c},a) = \frac{1}{N_{\omega} * N_{d}^{2}} \sum_{\omega} \widetilde{d}(\omega,a)^{H} K(\omega) \widetilde{d}(\omega,a)$$

with  $\widetilde{d}(\omega, \mathbf{a}) = \exp\left(i\omega r_{a/c}\right)$  the complex model vector and  $r_a$  the distance to the trial source a

#### Observed phase field after an icequake





#### Matched-field-processing (MFP)

- Consider 1 second-long signals
- Calculate the cross-spectral density matrix as

 $K(\omega) = d(\omega)d^{H}(\omega)$ 

with  $d(\omega)$  the complex data vector and H the Hermitian (conjugate) transpose

• Evaluate the match between the observed and modelled phases in a 4 dimensional space as

$$B_{Bartlett}(\omega_{c},a) = \frac{1}{N_{\omega} * N_{d}^{2}} \sum_{\omega} \widetilde{d}(\omega,a)^{H} K(\omega) \widetilde{d}(\omega,a)$$

with  $\widetilde{d}(\omega, \mathbf{a}) = \exp\left(i\omega r_{a/c}\right)$  the complex model vector and  $r_a$  the distance to the trial source a Example of a well identified icequake





#### Matched-field-processing (MFP)

- Consider 1 second-long signals
- Calculate the cross-spectral density matrix as

 $K(\omega) = d(\omega)d^{H}(\omega)$ 

with  $d(\omega)$  the complex data vector and H the Hermitian (conjugate) transpose

• Evaluate the match between the observed and modelled phases in a 4 dimensional space as

$$B_{Bartlett}(\omega_{c},a) = \frac{1}{N_{\omega} * N_{d}^{2}} \sum_{\omega} \widetilde{d}(\omega,a)^{H} K(\omega) \widetilde{d}(\omega,a)$$

with  $\widetilde{d}(\omega, \mathbf{a}) = \exp\left(i\omega r_{a/c}\right)$  the complex model vector and  $r_a$  the distance to the trial source a

#### Scheme for finding maxima

- Use of a gradient-based minimization algorithm (Nelder-Mead optimization)
- Efficiently converge to the best match
- Use 29 starting points to
  - Increase the likelihood that the global best match is found
  - Keep track of local best matches





#### Coherent wavefield



More incoherent wavefield





#### Coherent wavefield



More incoherent wavefield



Using realistic values:

We save all sources (i.e. up to 29) found every second

Up to 50+ millions potential locations per day



- Phase velocity
   [1500-3600 m.sec<sup>-1</sup>]
- Source positions
   ± 400m from array center in (x,y,z) 7





There is always some degree of coherence in the observed phase field !







### High MFP Outputs reflect crevasses





f = 17 Hz

 $v_c \approx 1600 \text{ m/s}$  $\lambda \approx 100 \text{ m}$ 





f = 17 Hz

 $v_c \approx 1600 \text{ m/s}$  $\lambda \approx 100 \text{ m}$ 

Hyper-resolution, i.e. resolution beyond the diffraction limit ?

Photo-activated localization microscopy

Rust et al., 2006; Betzig et al., 2006











D116












3D investigation: event depths ? Difficulty: 2D array, mostly surface waves





3D investigation: event depths ? Difficulties: 2D array, mostly surface waves





3D investigation: event depths ? Difficulties: 2D array, mostly surface waves





3D investigation: event depths







- Use 29 starting points to
  - Increase the likelihood that a global best match is found
  - Allow keeping track of local best matches









Nanni et al., 2022



• Along-flow geometry

- $\sim$  50m width of source location
  - Due to seismic wavelength? (300m at 5Hz)
  - Spread sources?

WE ARE ABLE TO LOCATE SUBGLACIAL WATER FLOW

### Spatio-temporal dynamics



### From distributed ...



### From distributed ...



### From distributed ... to localized



### From distributed ... to localized



### From distributed ... to localized



WE ARE CAPABLE OF CAPTURING SUBGLACIAL HYDROLOGY DYNAMICS

# Spatial dynamics and hydraulic properties



# Spatial dynamics and hydraulic properties



# Spatial dynamics and hydraulic properties



### From inefficient to efficient?



### Use arrays of sensors for observing spatial and temporal changes

#### The Argentière Glacier (France)



#### The Lemon Creek Glacier (Alaska)



### Use arrays of sensors for observing spatial and temporal changes

The Lemon Creek Glacier (Alaska)



Labedz et al., JGR, 2022

# Subglacial hydrology « Tremors » generated by subglacial water flow



Bartholomaus et al., 2015



### Understanding the physical process behind the « tremor »

source

Mendenhall Glacier, Alaska







Evolution of physical variables like pressure and size can be quantified using seismic and subglacial discharge observations







Evolution of physical variables like pressure and size can be quantified using seismic and subglacial discharge observations





Subglacial conduit flow evolves at constant pressure gradient/varying radius



Subglacial conduit flow transitions from varying to constant pressure gradient



Labedz et al., 2022

22



### PERSPECTIVES

### Target representative areas while ensuring imaging capabilities



### Use arrays of sensors for observing spatial and temporal changes



Gimbert et al., SRL, 2021; Nanni et al., PNAS, 2021; Nanni et al., GRL, 2022

Labedz et al., JGR, 2022



River









**Open surface flow (e.g. river)** 

$$|P(f)| \propto W u_*^{14/3} \qquad \longleftarrow \qquad P \quad \sim Q^{1.4}$$

Closed conduit (e.g. subglacial channel)



$$P_w \propto \Gamma u_*^{14/3}$$
 with  $u_* = \sqrt{gRS}$   
 $P_w \propto R^{10/3} S^{7/3}$ 

R: hydraulic radius

 $R = A/\Gamma$ 

S : hydraulic pressure  
gradient  
$$S = -\frac{1}{\rho g} \frac{\partial p}{\partial x} + \tan \theta$$

**Open surface flow (e.g. river)** 

$$|P(f)| \propto W u_*^{14/3} \qquad \longleftarrow \qquad P \quad \sim Q^{1.4}$$

### Closed conduit (e.g. subglacial channel)



R : hydraulic radius  $R = A/\Gamma$ 

S : hydraulic pressure gradient  $S = -\frac{1}{\rho g} \frac{\partial p}{\partial x} + \tan \theta$ 

$$P_{W} \propto \Gamma u_{*}^{14/3} \text{ with } u_{*} = \sqrt{gRS}$$

$$P_{W} \propto R^{10/3} S^{7/3}$$

$$Q = AU \text{ with } U \propto R^{2/3} S^{1/2}$$

$$Manning, 1891$$

$$Q \propto R^{8/3} S^{1/2}$$

**Open surface flow (e.g. river)** 

$$|P(f)| \propto W u_*^{14/3} \qquad \longleftarrow \qquad P \quad \sim Q^{1.4}$$

### Closed conduit (e.g. subglacial channel)



R : hydraulic radius  $R = A/\Gamma$ 

S : hydraulic pressure gradient  $S = -\frac{1}{\rho g} \frac{\partial p}{\partial x} + \tan \theta$ 

$$P_{W} \propto \Gamma u_{*}^{14/3} \text{ with } u_{*} = \sqrt{gRS}$$

$$P_{W} \propto R^{10/3} S^{7/3}$$

$$Q = AU \text{ with } U \propto R^{2/3} S^{1/2}$$

$$P_{W} \propto R^{-82/9} Q^{14/3}$$

$$P_{W} \propto S^{41/24} Q^{5/4}$$

$$Q \propto R^{8/3} S^{1/2}$$

**Open surface flow (e.g. river)** 

$$|P(f)| \propto W u_*^{14/3} \qquad \longleftarrow \qquad P \quad \sim Q^{1.4}$$

### Closed conduit (e.g. subglacial channel)



R : hydraulic radius  $R = A/\Gamma$ 

S : hydraulic pressure gradient  $S = -\frac{1}{\rho g} \frac{\partial p}{\partial x} + \tan \theta$ 

$$P_{w} \propto \Gamma u_{*}^{14/3} \text{ with } u_{*} = \sqrt{gRS}$$

$$P_{w} \propto R^{10/3} S^{7/3}$$

$$Q = AU \text{ with } U \propto R^{2/3} S^{1/2}$$

$$Manning, 1891$$

$$Q \propto R^{8/3} S^{1/2}$$
Environments
$$F_{w} \propto Q$$

$$P_{w} \propto Q$$

$$F_{w} \propto Q$$

$$F_{w} \propto Q$$

End-member cases  
Varying pressure  
$$P_w \propto Q^{14/3}$$
 STRONG scaling  
 $\neq$   
Varying size  
 $P_w \propto Q^{5/3}$  WEAK scaling

# Water flow causes ground shaking



### **Open surface flow (e.g. river)** Theory :

 $P \sim Q^{1.4}$ Seismic power Discharge

Gimbert et al., 2014


### Understanding the physical process behind the « tremor »

source

Mendenhall Glacier, Alaska







Evolution of physical variables like pressure and size can be quantified using seismic and subglacial discharge observations



#### Understanding the physical process behind the « tremor » source





Evolution of physical variables like pressure and size can be quantified using seismic and subglacial discharge observations





Subglacial conduit flow evolves at constant pressure gradient/varying radius



Subglacial conduit flow transitions from varying to constant pressure gradient



Labedz et al., 2022





### Conclusion

1- Understand the physical process behind the « tremor » source

Turbulent-flow-induced force fluctuations

Water pressure and conduit size changes can be inferred from seismic observations

The Lemon Creek

Glacier (Alaska)

Gimbert et al., 2014; Gimbert et al., 2016; Nanni et al., 2020

2- Use arrays of sensors for observing spatial and temporal changes

The Argentière Glacier (France)



Gimbert et al., 2021; Nanni et al., 2021; Nanni et al., 2022





### Perspectives



Can we still image distributed sources with a much coarser array ?



Gimbert et al., 2021; Nanni et al., 2021; Nanni et al., 2022

## Seismic array response with random phases



# Very low phase coherence: starting points location

*MFP out*. ∈ [0 0. 01]



## How patterns evolve with frequency



## How patterns evolve with frequency











## Evidences for diffracting material



### Crevasses



## Phase velocity distribution



# Phase velocity distribution



## From distributed ... to localized



#### CAPABLE OF CAPTURING SUBGLACIAL HYDROLOGY DYNAMICS



2D correlation coefficient with final pattern

%

(Nanni et al., 2021 PNAS)



## Observing the inefficient drainage system



We can observe **<u>distributed</u>** water flow in the cavities with seismology

Previously thought to be noise-free

# Implication for subglacial hydrology dynamics

- Do we observe cavities only?
- Do cavities dominate the drainage system?

#### **Modelling** subglacial hydrology with Elmer/Ice-GlaDS coupling by A. Gilbert



## Spectrograms

