



NANYANG
TECHNOLOGICAL
UNIVERSITY

UNIVERSITÉ
CÔTE D'AZUR



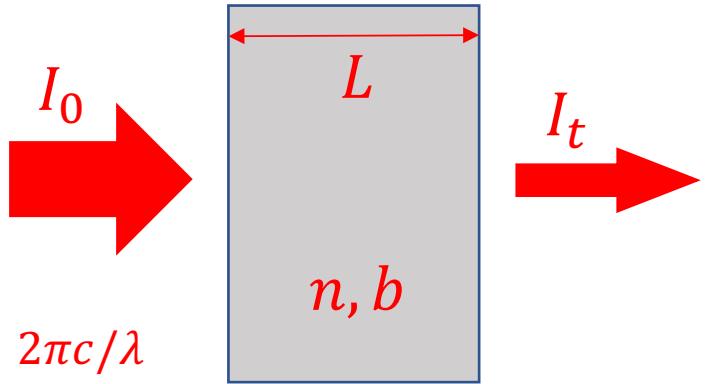
Forward Scattering of Light: Cooperativity, Superflash, and More

David Wilkowski



GdR Complexe Annual Workshop: Dec 7th 2022

Beer-Lambert's law: $I_t(\omega) = I_0(\omega)e^{-b(\omega)}$



For the electric field:

Optical frequency: $\omega = kc = 2\pi c/\lambda$

$$E_t(\omega) = E_0(\omega)\exp[in(\omega)kL] = E_0(\omega)\exp\left[-\frac{b(\omega)}{2} + i\phi(\omega)\right]\exp(ikL)$$

With a two-level atom (RWA): $n(\omega) = 1 + \rho\alpha(\omega)/2$

In a dilute medium $\rho\lambda^3 \ll 1$

Atomic polarizability

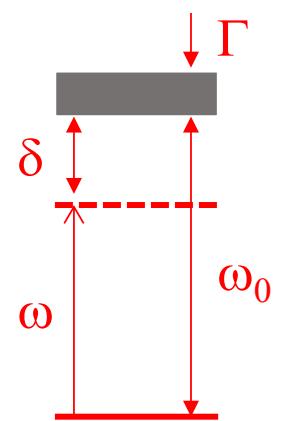
$$\alpha(\omega) = -\frac{3\pi}{k^3} \frac{\Gamma}{\delta + i\Gamma/2}$$

$$b = \text{Im}\{\alpha\}\rho kL \xrightarrow{\text{Optical theorem}}$$

$$\phi = \frac{\text{Re}\{\alpha\}}{2} \rho kL$$

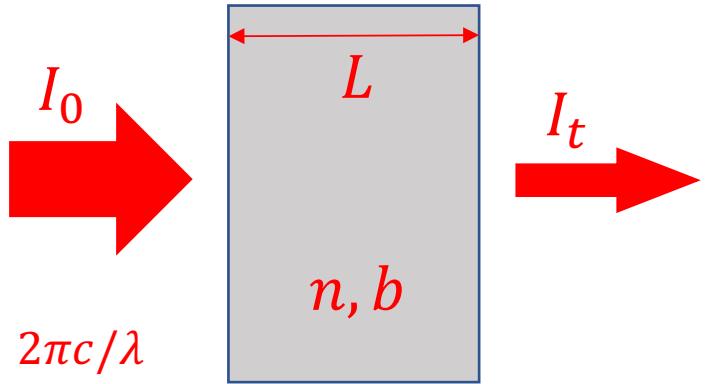
Scattering cross section

$$\delta = \omega - \omega_0$$



Forward Scattering Field

Beer-Lambert's law: $I_t(\omega) = I_0(\omega)e^{-b(\omega)}$



Optical frequency: $\omega = kc = 2\pi c/\lambda$

For the electric field:

$$E_t(\omega) = E_0(\omega)\exp[in(\omega)kL] = E_0(\omega)\exp\left[-\frac{b(\omega)}{2} + i\phi(\omega)\right]\exp(ikL)$$

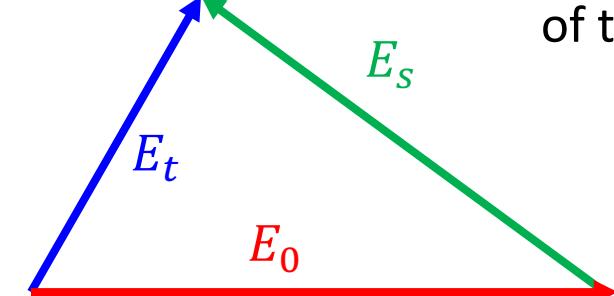
Coherent superposition of scalar fields:

$$E_t(t) = E_0(t) + E_s(t)$$

E_t : the transmitted field

E_0 : the incident field

E_s : the forward scattering field



Geometrical representation
of the fields in the complex plane



Direct Observation of the Forward Scattering Field: Flash Effect

Superflash Effect: $I_s|_{\text{sta}} > I_0|_{\text{sta}}$

Cooperative Pulse Train

Flash in Λ -Scheme

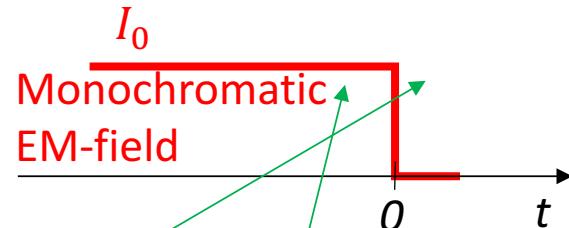
Outlook



Magneto-optical trap: 10^9 strontium atoms

Direct Observation of the Forward Scattering Field

$$E_t(t) = E_0(t) + E_s(t) \rightarrow E_t(t) = \cancel{E_0(t)} + E_s(t)$$



$$E_s(0^+) = E_s \Big|_{\text{sta}} \equiv E_s = E_t - E_0 = E_0 \left[\exp\left(-\frac{b}{2} + i\phi\right) - 1 \right]$$

Medium response time has to be not “too fast”!

Atoms with large resonance quality factor: $\frac{\Gamma}{\omega_0} \sim 10^{-11}$

If $\delta \gg \Gamma \rightarrow (\phi, b) \sim 0 \rightarrow E_s \sim 0$

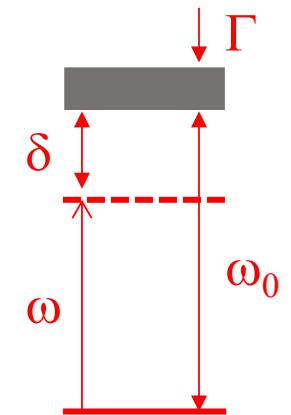
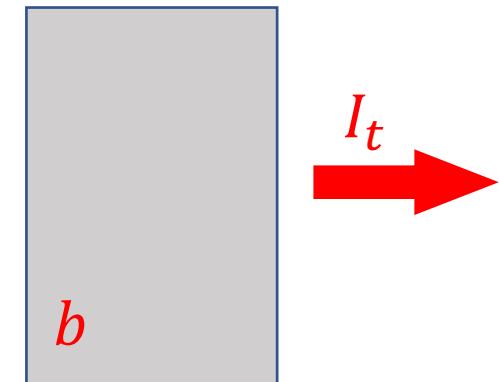
$$\delta = \omega - \omega_0$$

If $\delta \ll \Gamma$ and $b \gg 1 \rightarrow E_t = 0, E_s \sim -E_0$

$$b = \text{Im}\{\alpha\} \rho k L$$



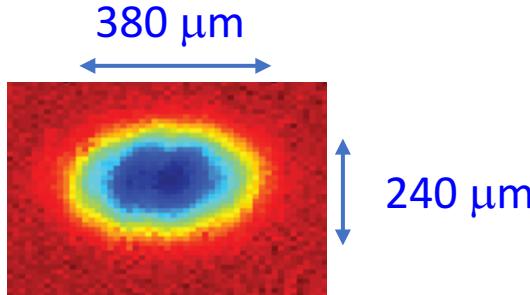
$$\phi = \frac{\text{Re}\{\alpha\}}{2} \rho k L$$



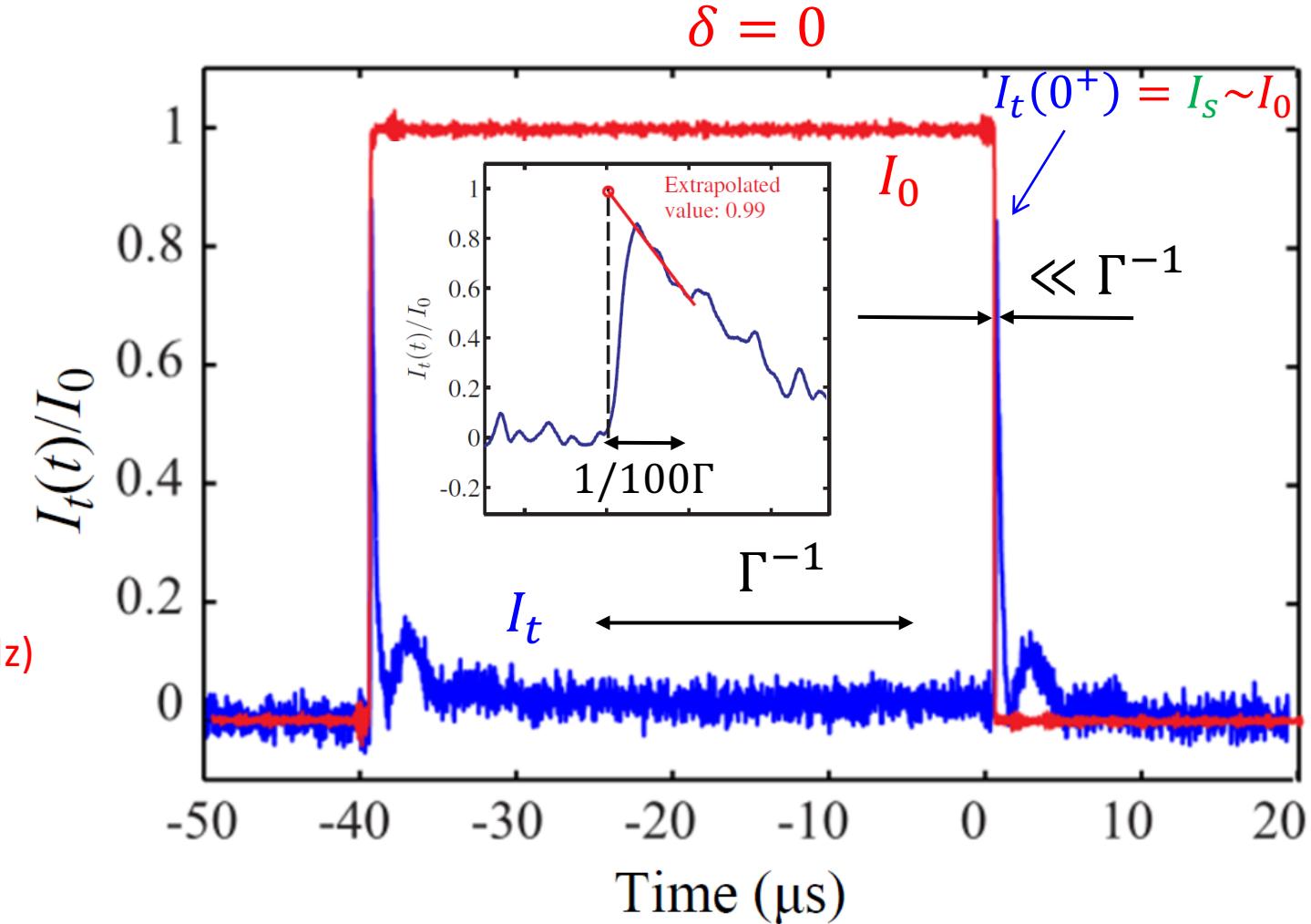
$$\alpha(\omega) = -\frac{3\pi}{k^3} \frac{\Gamma}{\delta + i\Gamma/2}$$

Flash Effect

Ultracold Strontium gas

Atoms number: $N = 3 \cdot 10^8$ Density: $\rho \sim 5 \cdot 10^{11} \text{ atoms/cm}^3$ Dilute medium: $\rho\lambda^3 \sim 0.1$ Temperature: $3 \mu\text{K} \rightarrow k\bar{v} = 3.4 \Gamma$ Optical thickness: $b_0(\bar{v}) = 19 \left(\frac{\Gamma}{2\pi}\right) \sim 7.5 \text{ kHz}$

$$\begin{array}{ccc} b_0(0) & = & 120 \\ \delta = 0 & \nearrow & \nwarrow \\ T = 0 & & \end{array}$$

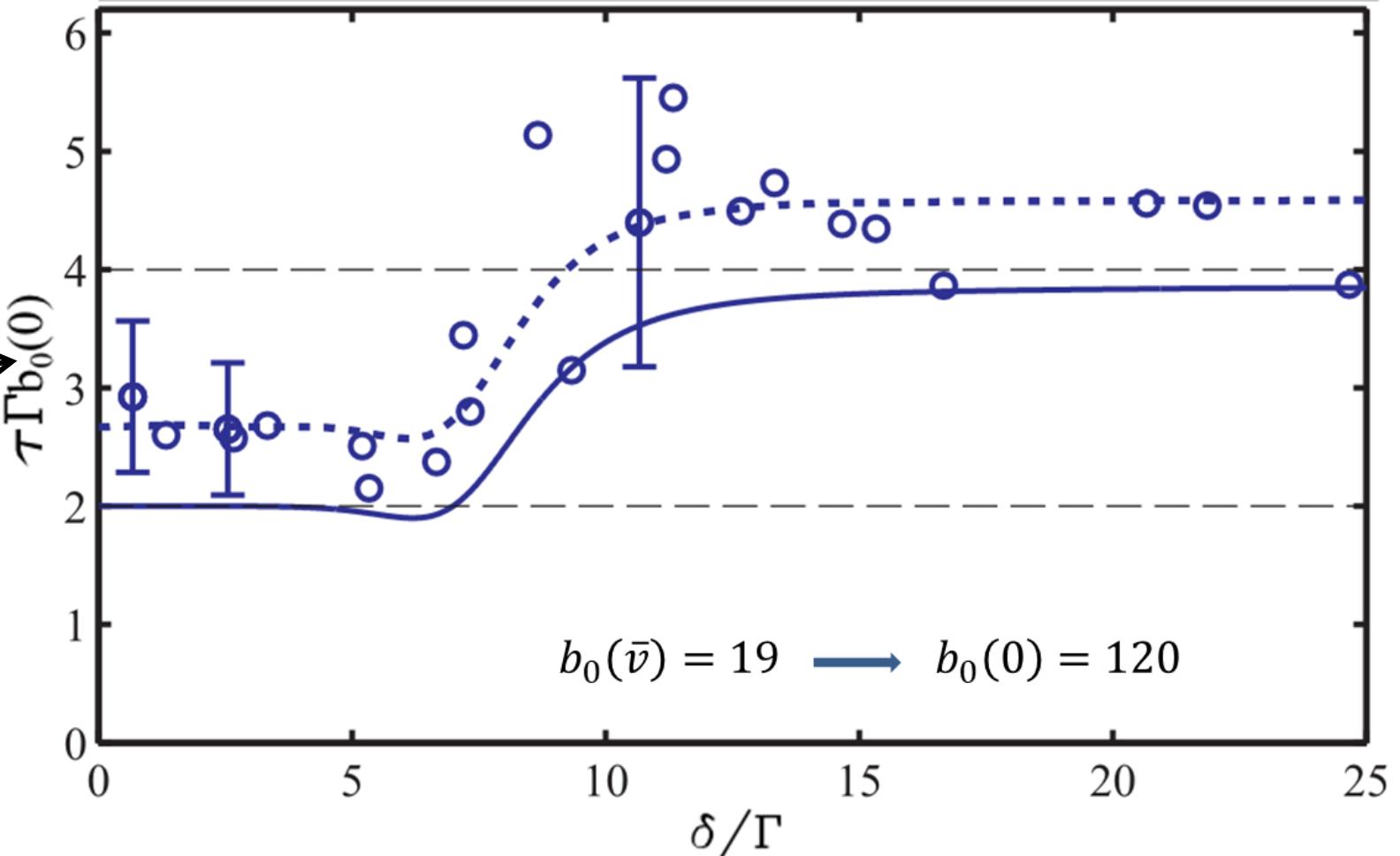


$$\tau = \frac{I(0^+)}{dI(0^+)/dt}$$

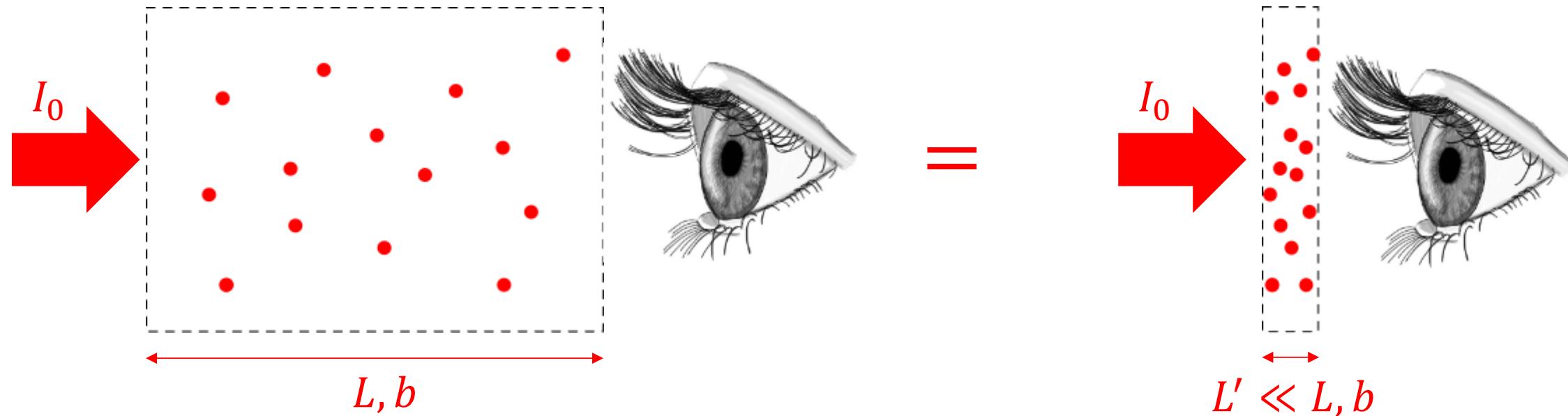
$$T = 0$$

$$\delta = 0 \rightarrow \tau \Gamma b_0(0)$$

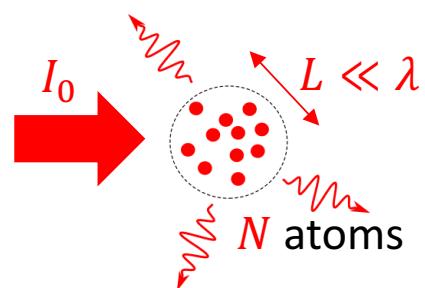
$$\tau \sim \frac{1}{b\Gamma} \ll \frac{1}{\Gamma}$$



Flash Effect vs Superradiance

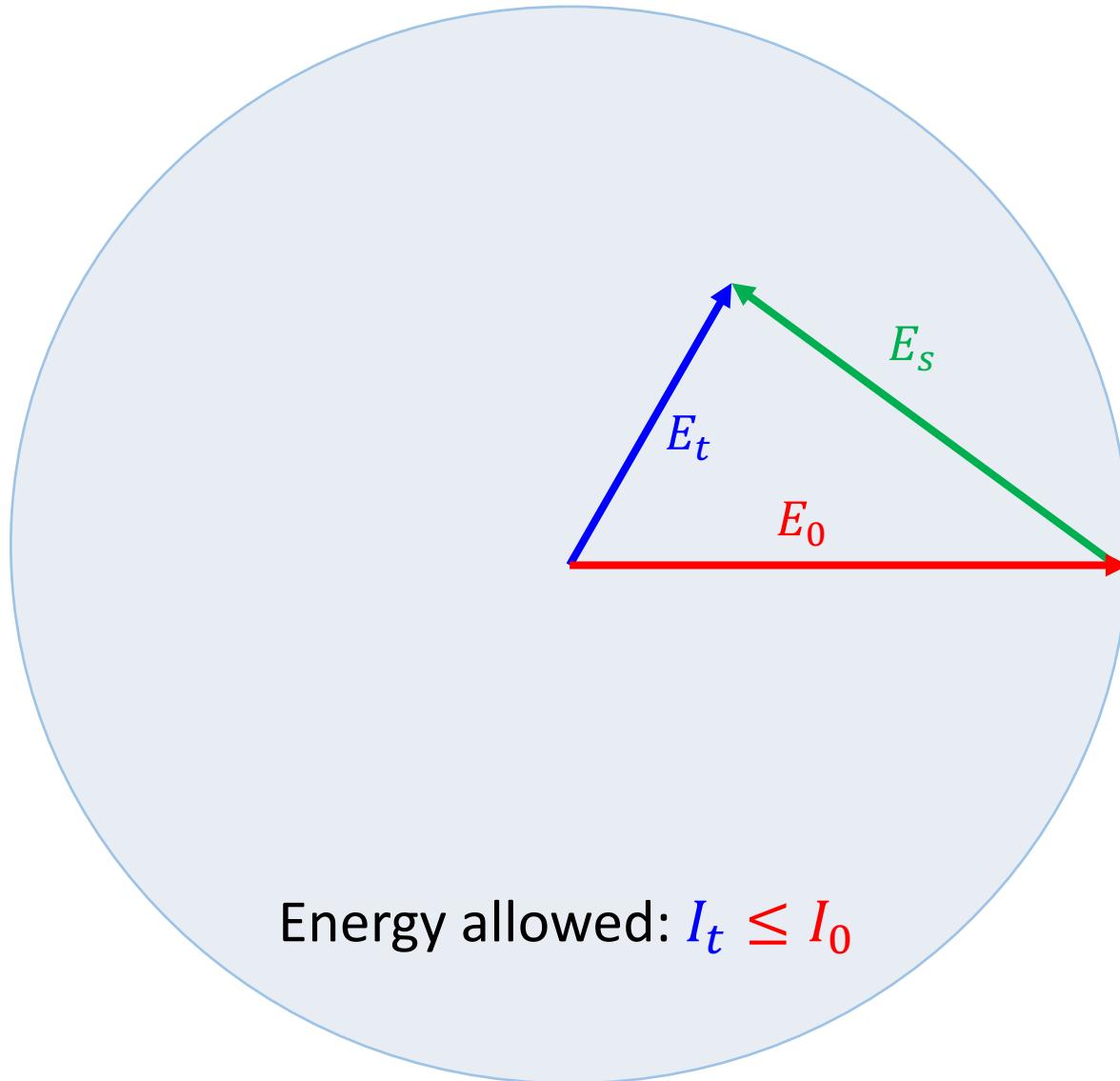


Optical thickness b \leftrightarrow Effective atoms number



Superradiance: $\tau \sim 1/N\Gamma \leftrightarrow$ Flash $\tau \sim 1/b\Gamma$

Flash is a cooperative emission in the forward direction

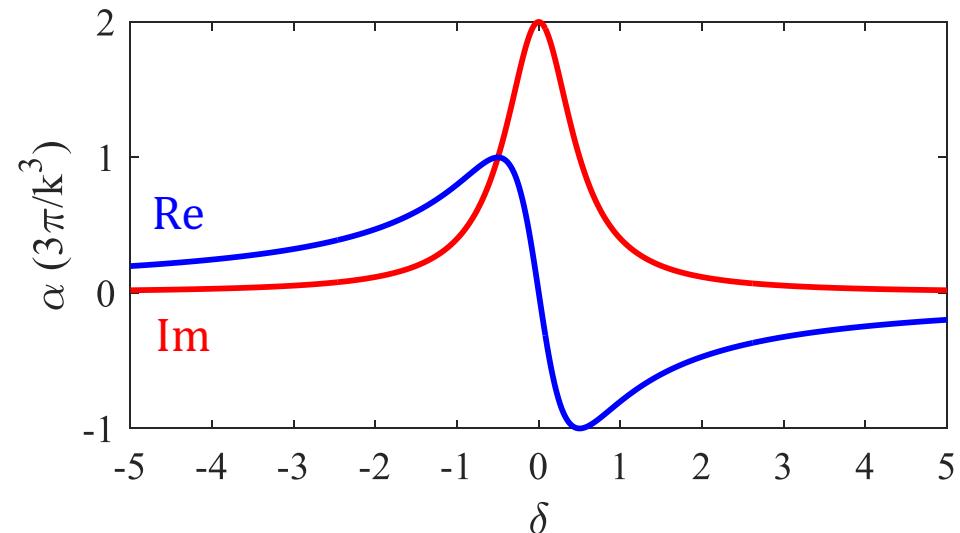


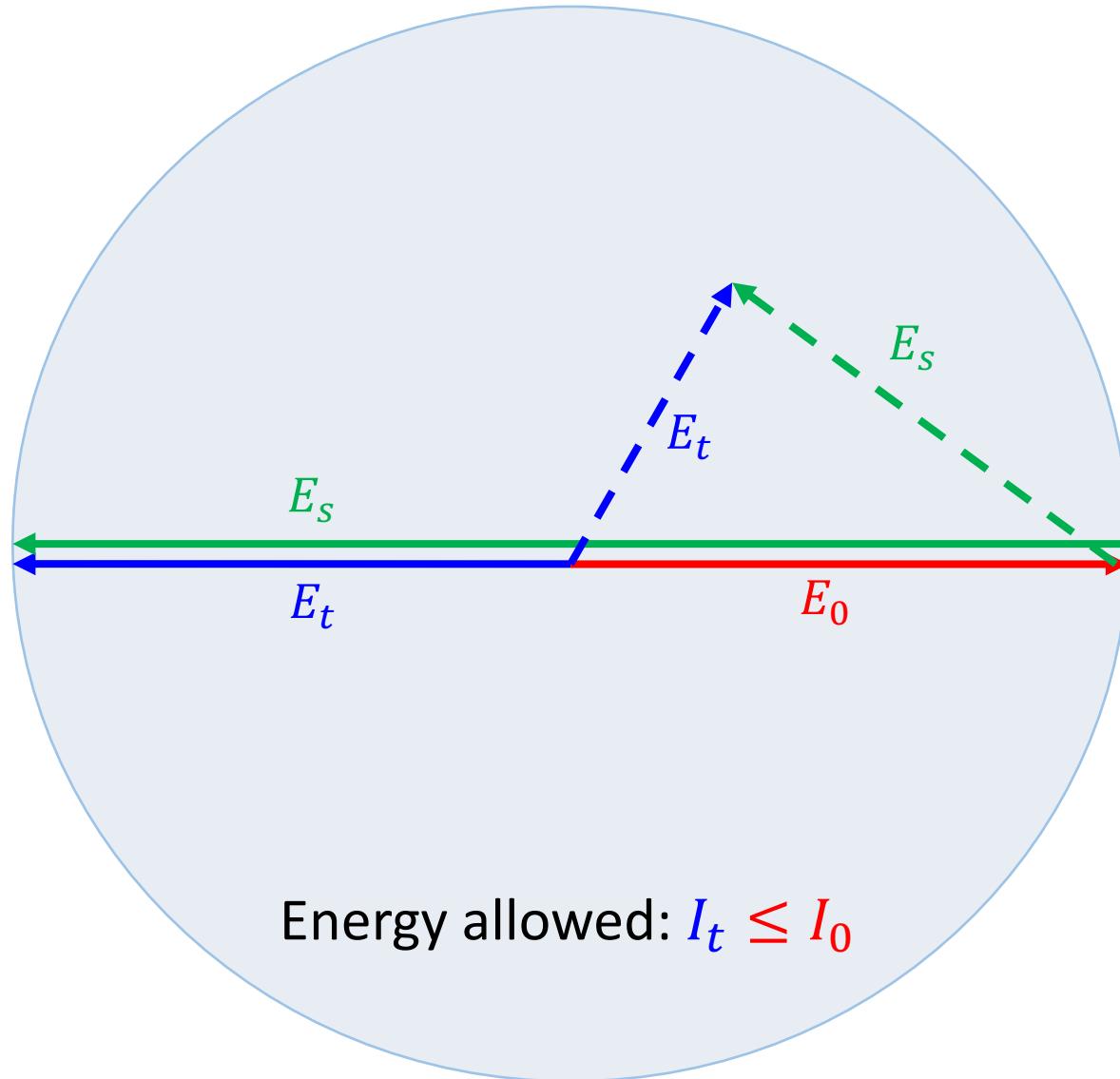
$$E_s(\omega) = E_0(\omega) \left[\exp\left(-\frac{b}{2} + i\phi\right) - 1 \right]$$

Max. value: $\exp\left(-\frac{b}{2} + i\phi\right) \rightarrow -1$

So we need: $b \rightarrow 0$ and $\phi \rightarrow \pm\pi$

$$b = \text{Im}\{\alpha\}\rho k L \quad \phi = \frac{\text{Re}\{\alpha\}}{2} \rho k L$$



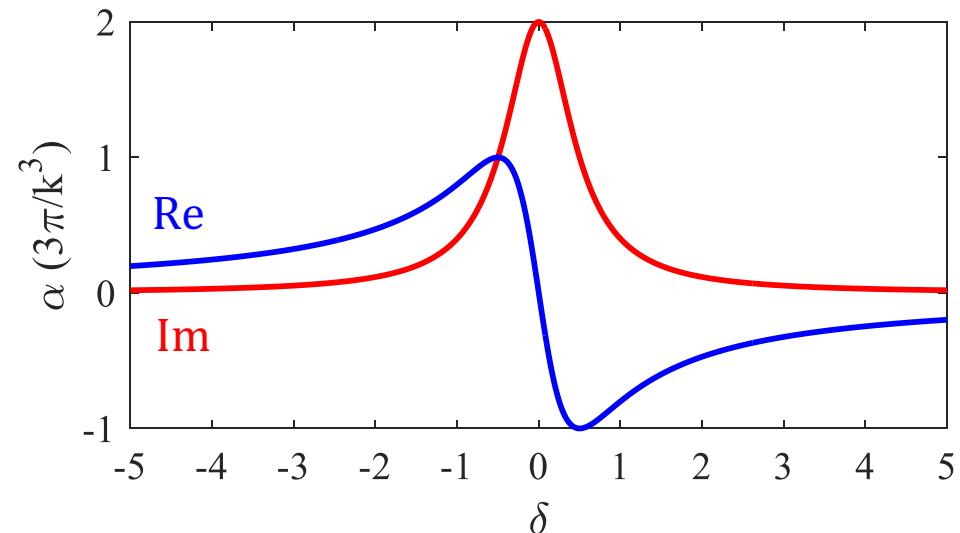


$$E_s(\omega) = E_0(\omega) \left[\exp\left(-\frac{b}{2} + i\phi\right) - 1 \right]$$

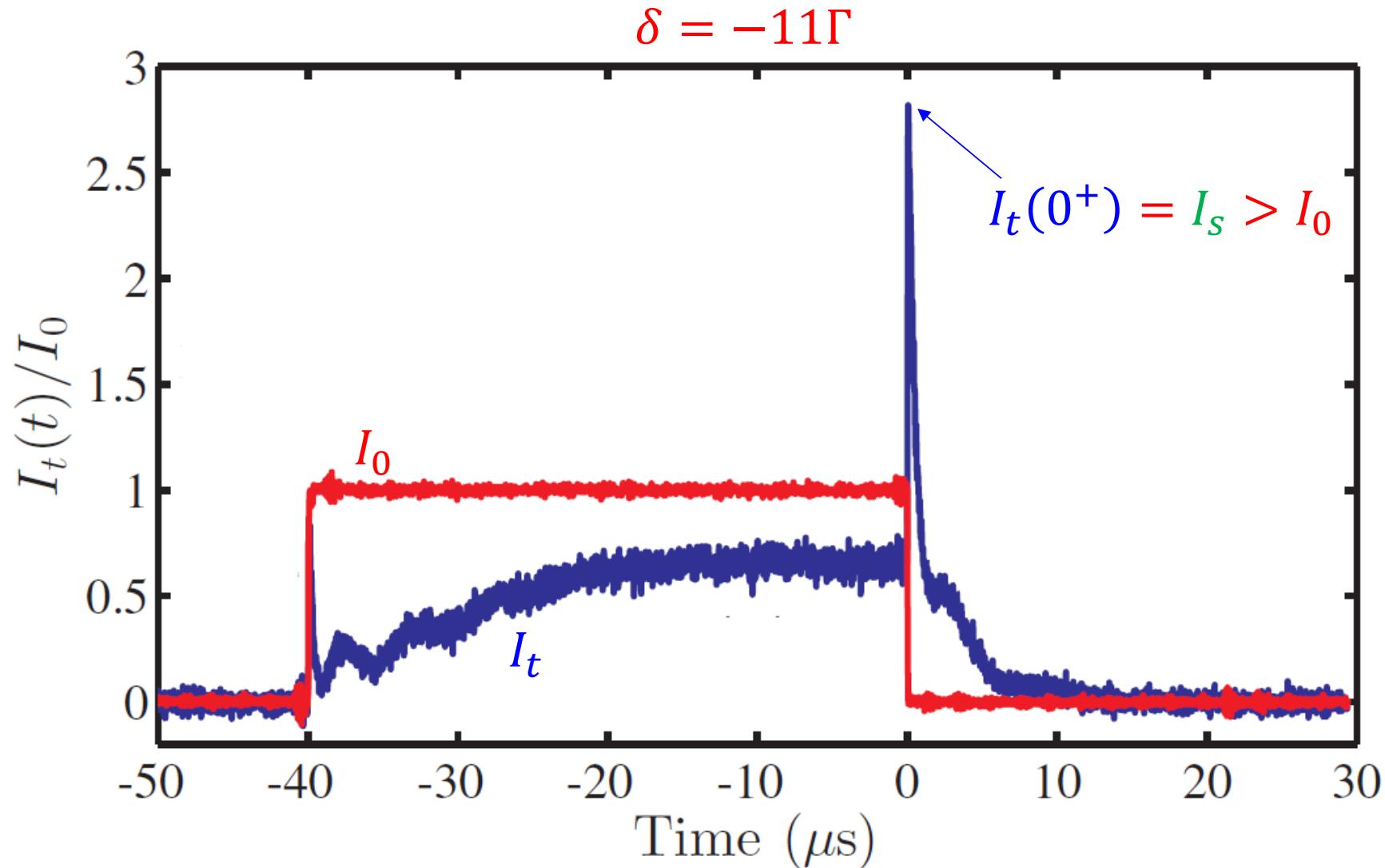
$$\text{Max. value: } \exp\left(-\frac{b}{2} + i\phi\right) \rightarrow -1$$

So we need: $b \rightarrow 0$ and $\phi \rightarrow \pm\pi$

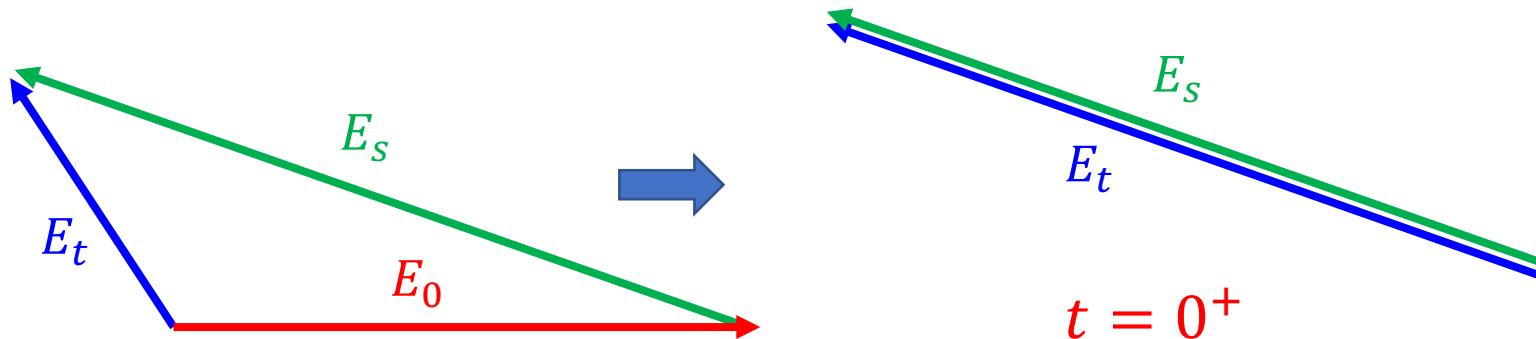
$$b = \text{Im}\{\alpha\}\rho k L \quad \phi = \frac{\text{Re}\{\alpha\}}{2} \rho k L$$



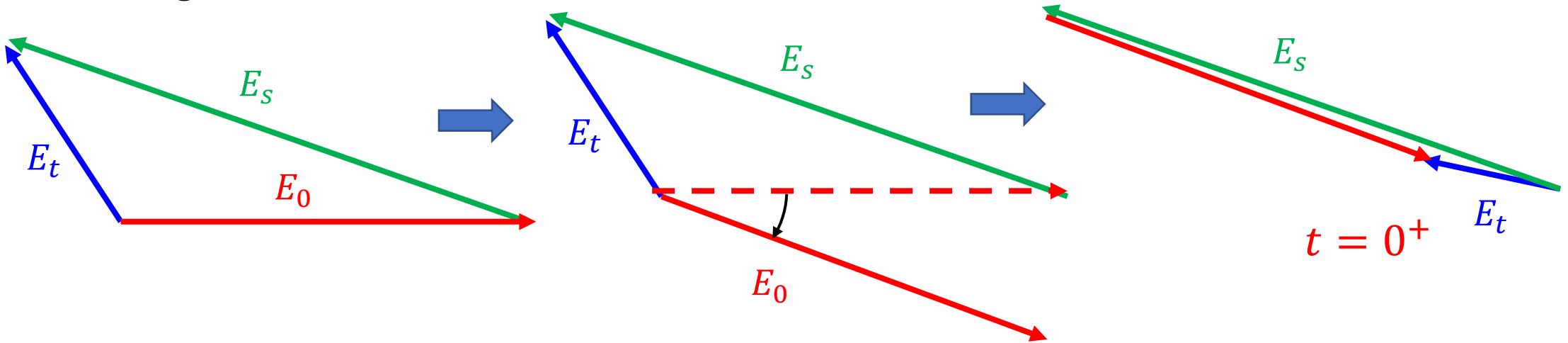
Superflash Effect



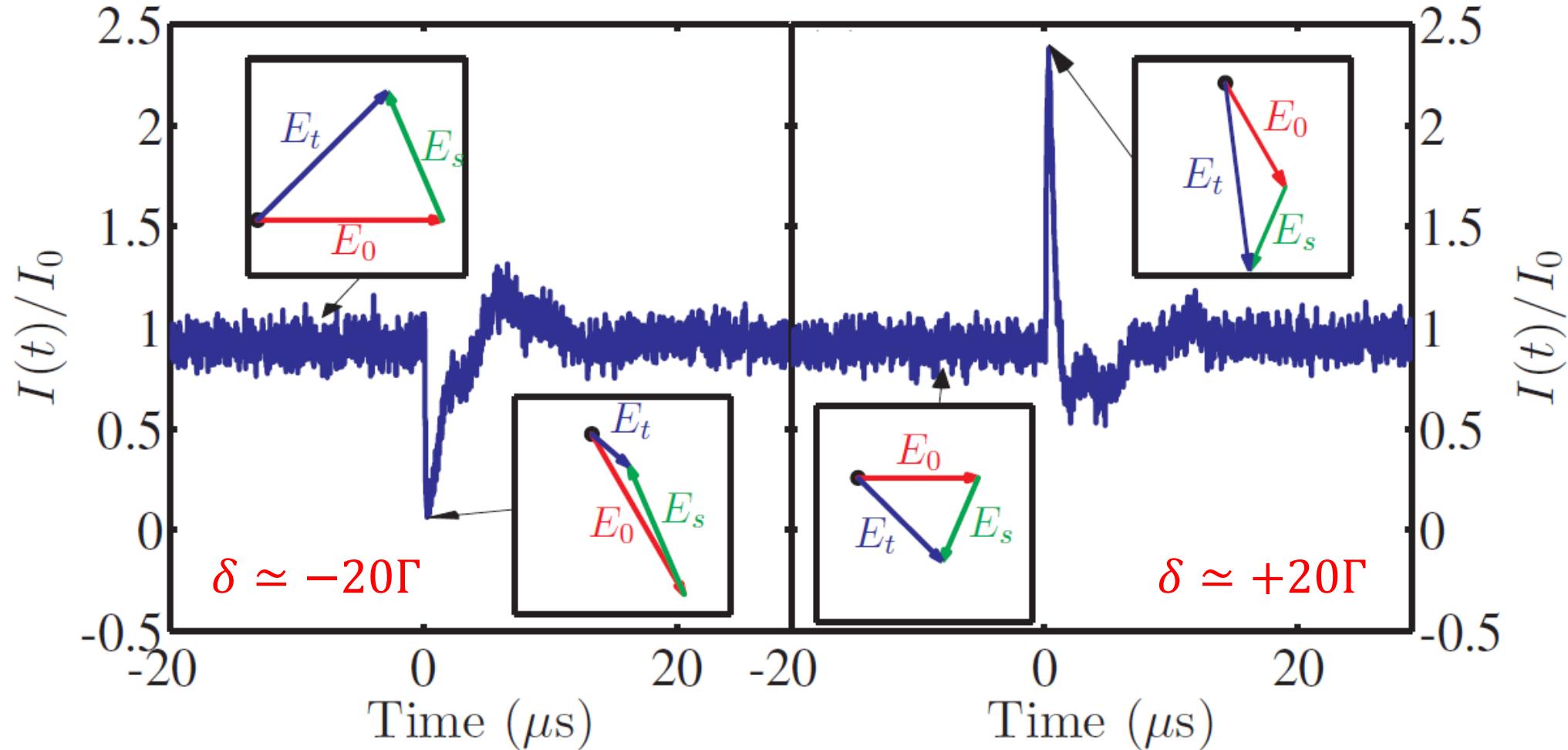
Switch off:

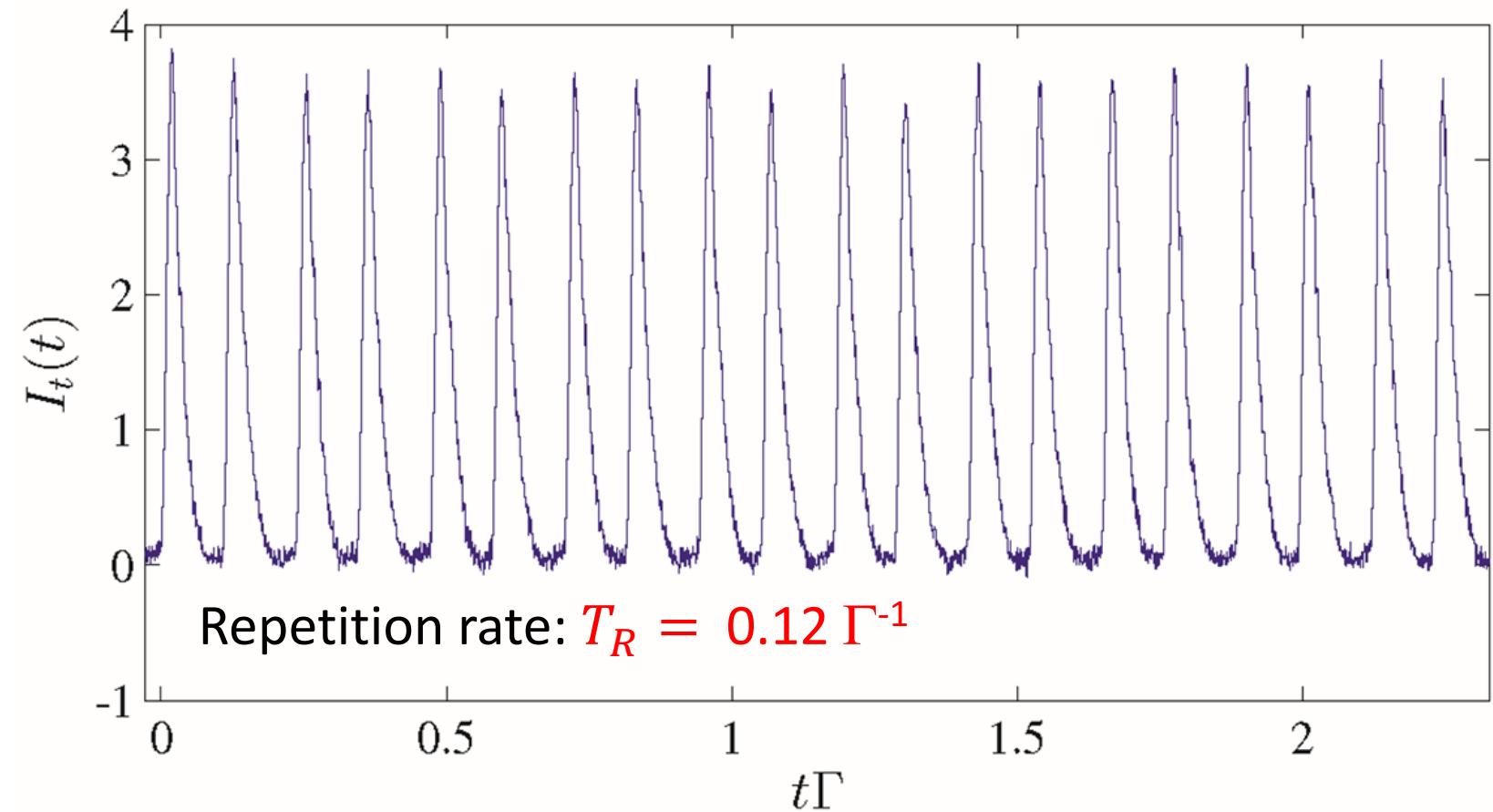
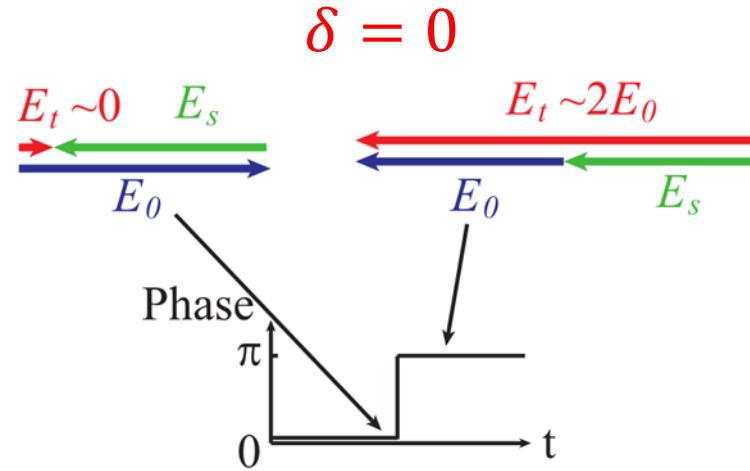


Phase change:

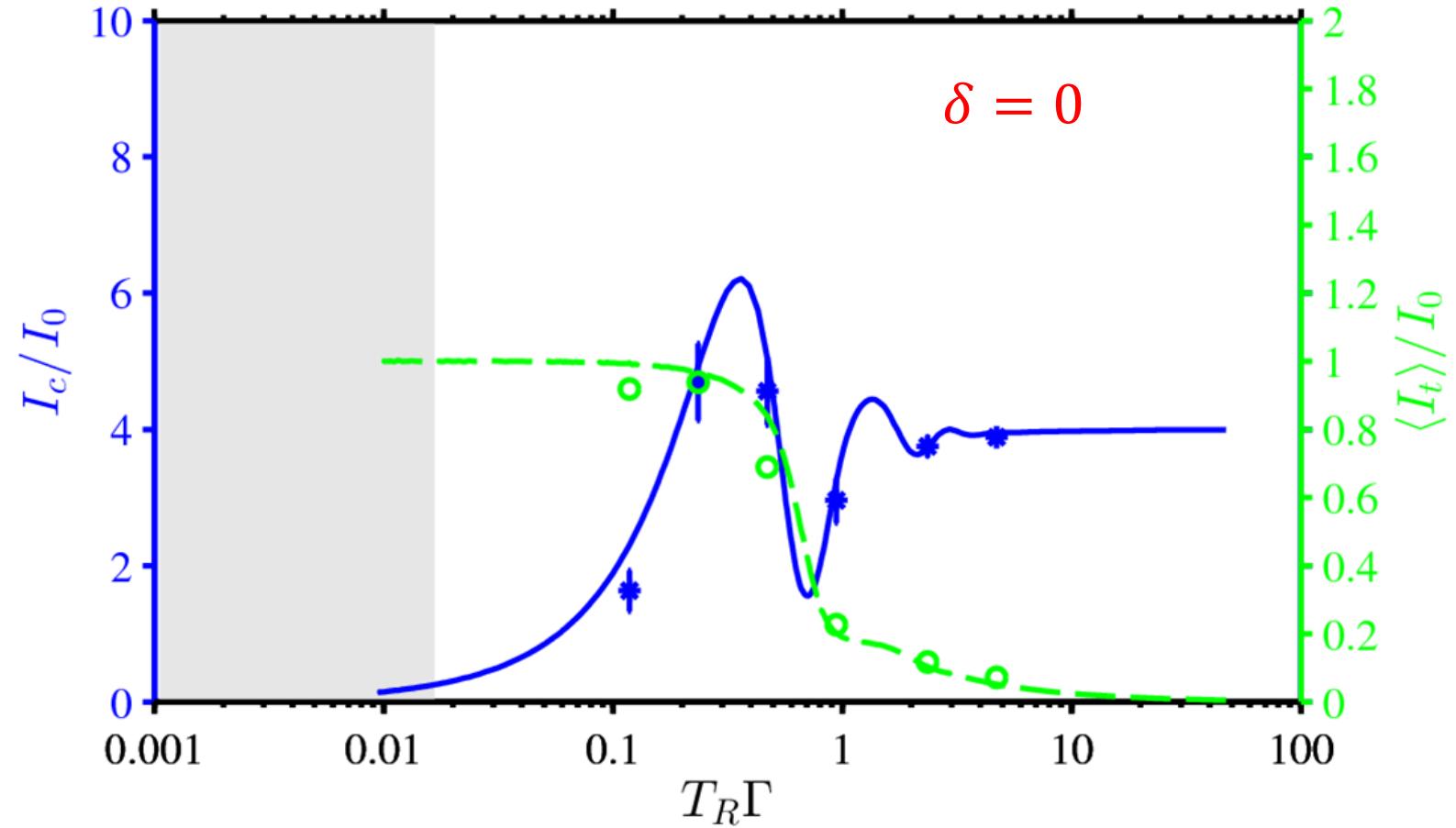


Phase change





Pulse Train: Figure of Merit



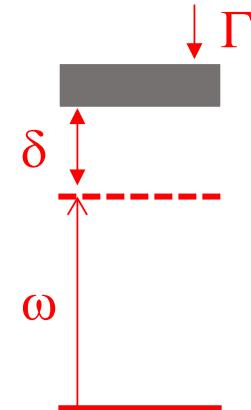
If the repetition rate $T_R < \Gamma^{-1}$ fluorescence is quenched

Two-level to Λ -scheme

Two-level: $E_t(t) = E_0(t) + E_s(t)$

$$\alpha = -\frac{3\pi}{k^3} \frac{\Gamma}{\delta + i\Gamma/2}$$

If $\delta = 0$ and $b \gg 1$ ($\phi \sim 0$), $E_s \sim -E_0$



Λ -scheme: $E_t(t) = E_0(t) + E_s(t) + E_{S/\Lambda}(t)$

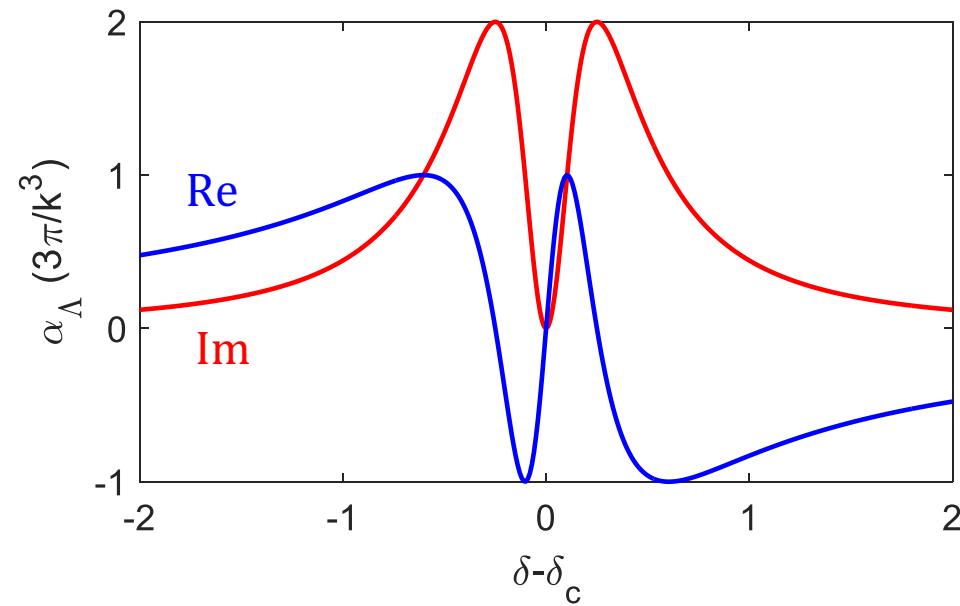
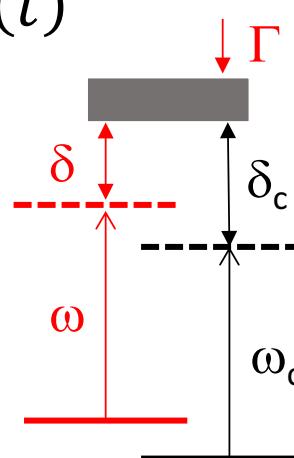
$$\alpha_\Lambda = \alpha \left(1 - \frac{|\Omega_c|^2/4}{(\delta + i\Gamma/2)(\delta - \delta_c)} \right)^{-1}$$

Narrow dark resonance: $\Gamma_d = |\Omega_c|^2 / \Gamma$

If $b \gg 1$, $\tau_{S/\Lambda} = b/\Gamma_d \gg \tau_S = 1/b\Gamma$

If $\delta = \delta_c = 0$ and $b \gg 1$ ($\phi = 0$), $E_s = -E_0$

and $E_t = E_0$, so $E_{S/\Lambda} = E_0$, and $I_t(0^+) = |E_s + E_{S/\Lambda}|_{\text{sta}}^2 = 0$



Two-level to Λ -scheme

Two-level: $E_t(t) = E_0(t) + E_s(t)$

$$\alpha = -\frac{3\pi}{k^3} \frac{\Gamma}{\delta + i\Gamma/2}$$

If $\delta = 0$ and $b \gg 1$ ($\phi \sim 0$), $E_s \sim -E_0$

Λ -scheme: $E_t(t) = E_0(t) + E_s(t) + E_{S/\Lambda}(t)$

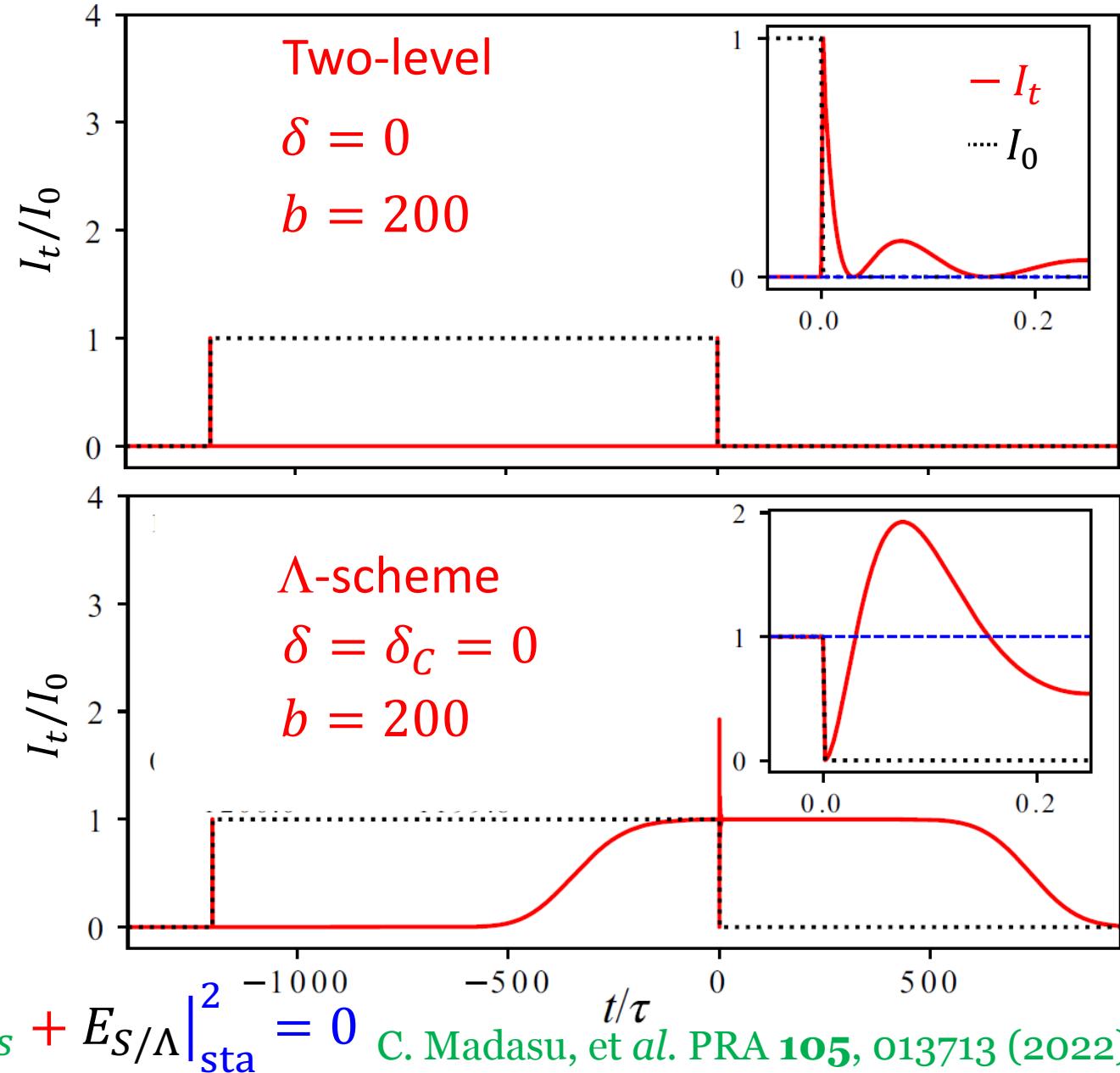
$$\alpha_\Lambda = \alpha \left(1 - \frac{|\Omega_c|^2/4}{(\delta + i\Gamma/2)(\delta - \delta_c)} \right)^{-1}$$

Narrow dark resonance: $\Gamma_d = |\Omega_c|^2 / \Gamma$

If $b \gg 1$, $\tau_{S/\Lambda} = b/\Gamma_d \gg \tau_S = 1/b\Gamma$

If $\delta = \delta_c = 0$ and $b \gg 1$ ($\phi \sim 0$), $E_s = -E_0$

and $E_t = E_0$, so $E_{S/\Lambda} = E_0$, and $I_t(0^+) = |E_s + E_{S/\Lambda}|_{\text{sta}}^2 = 0$



PRL 103, 093602 (2009)

PHYSICAL REVIEW LETTERS

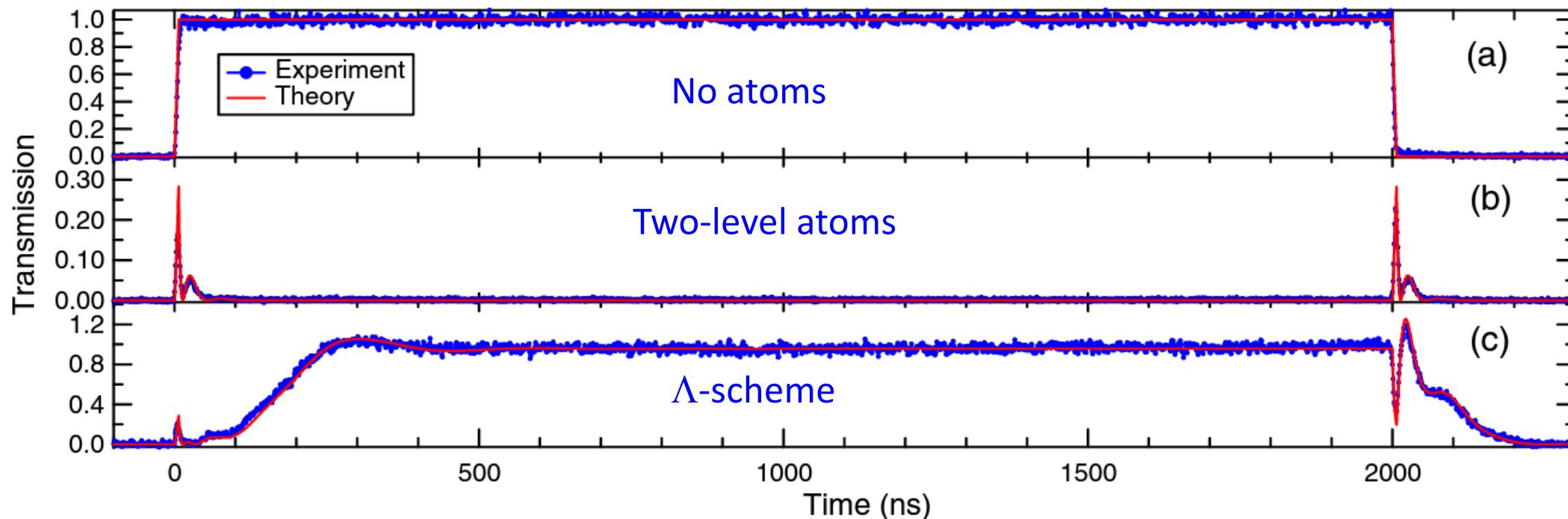
week ending
28 AUGUST 2009

Optical Precursors with Electromagnetically Induced Transparency in Cold Atoms

Dong Wei, J. F. Chen, M. M. T. Loy, G. K. L. Wong, and Shengwang Du*

Department of Physics, The Hong Kong University of Science and Technology, Clear Water Bay, Kowloon, Hong Kong, China

(Received 10 July 2009; published 28 August 2009)



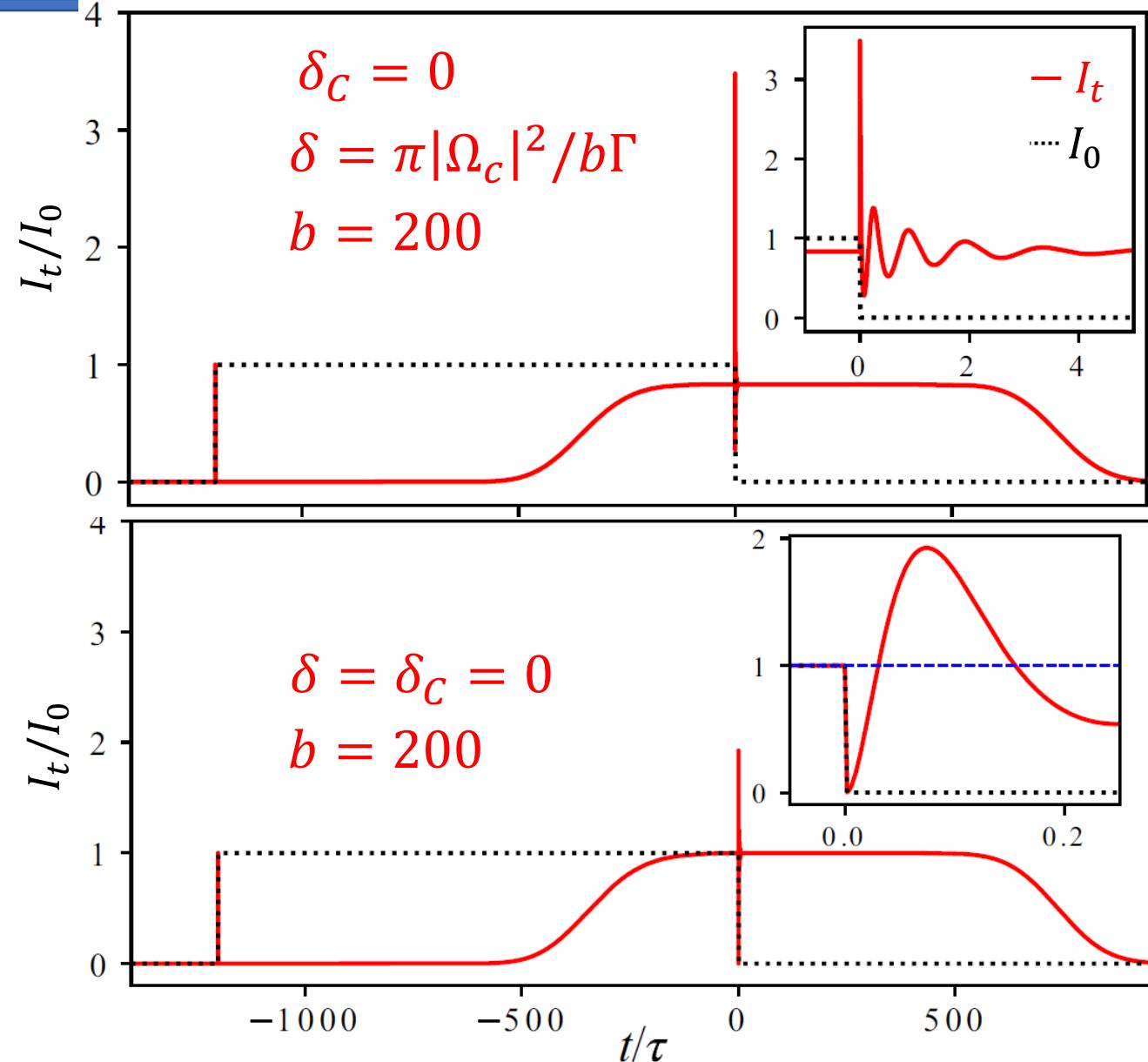
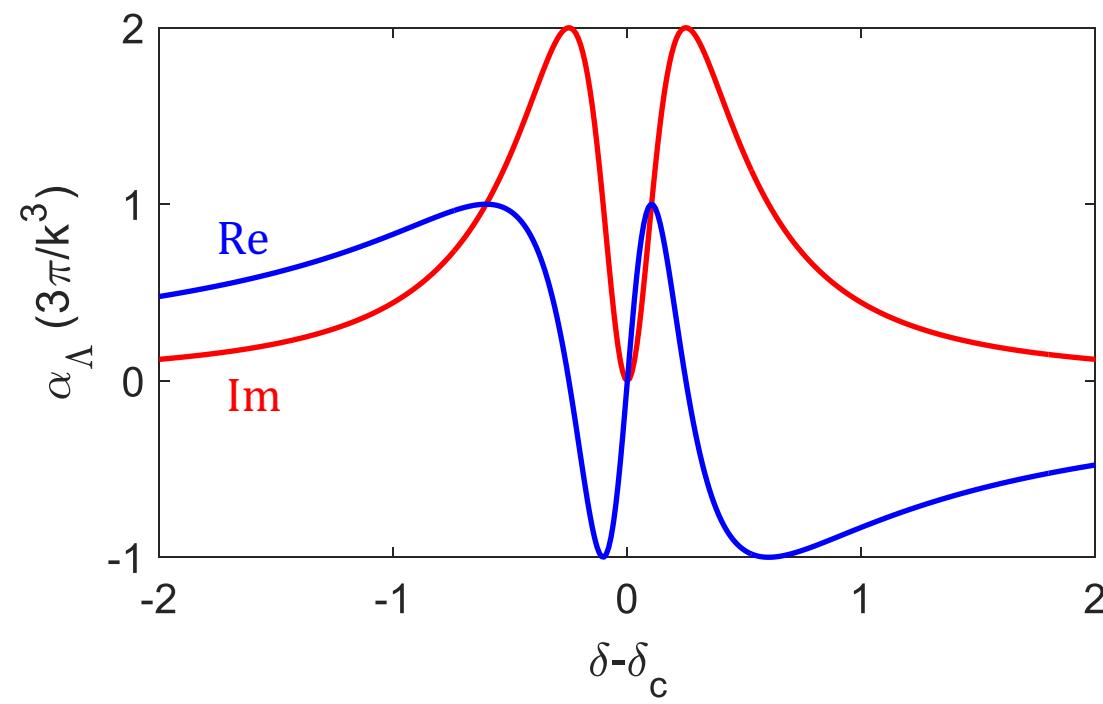
Phase Rotation in Λ -scheme

Λ -scheme: $E_t(t) = E_0(t) + E_s(t) + E_{S/\Lambda}(t)$

If $\delta = \delta_c = 0$, then $E_{S/\Lambda} = E_0$

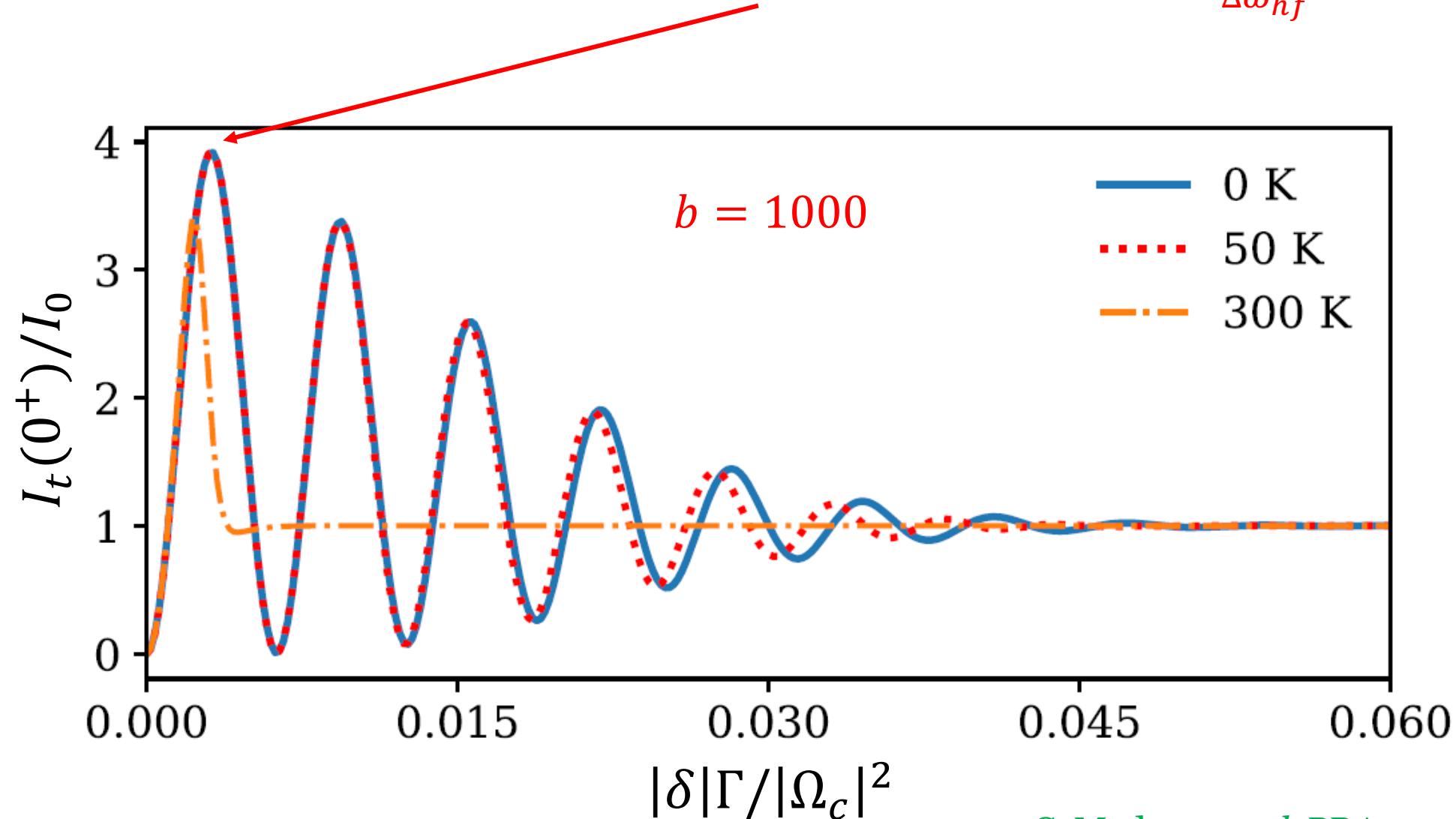
If $\delta = \pm\pi|\Omega_c|^2/b\Gamma \ll \Gamma$, then $E_{S/\Lambda} = -E_0$

$$I_t(0^+) = |E_s + E_{S/\Lambda}|_{\text{sta}}^2 = 4$$



Λ-scheme: Thermal effect

For Rb atoms: $\Gamma/2\pi = 6 \text{ MHz}$, $|\Omega_c| = \Gamma/10$, $|\delta|_\pi/2\pi \approx 300 \text{ Hz}$ and $\frac{|\delta|_\pi}{\Delta\omega_{hf}} = 5 \times 10^{-8}$





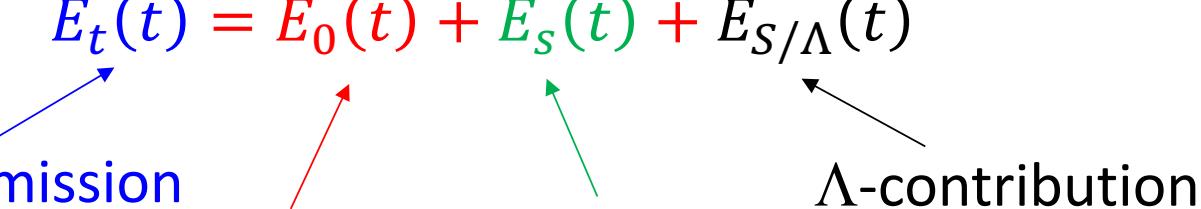
Conclusion and Outlook

Transient phenomena in the coherent transmission
of a optical thick medium with “slow” resonant response time.

Decomposition of the field as:

$$E_t(t) = E_0(t) + E_s(t) + E_{S/\Lambda}(t)$$

Transmission Incident Forward scattering Λ -contribution



E_s is “fast” $\sim 1/b\Gamma$. Similar to superradiance

$E_{S/\Lambda}$ is very “slow” $\sim b/\Gamma$. Slow light

$E_s, E_{S/\Lambda}$ can be extracted using the (super)flash effect, *i.e.* measurement of $I_t(0^+)$

Applications: Cooperative pulse generator, frequency sensing

Superflash and cooperative Pulse

Kwong Chang-Chi

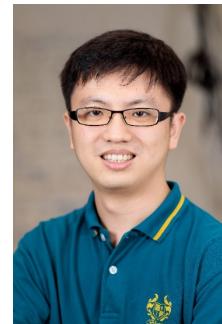
Kanhaiya Pandey

Mysore Pramod

Tao Yang

Dominique Delande

Romain Pierrat



C. C. Kwong, et al., PRL **113**, 223601 (2014)

C. C. Kwong, et al. PRL **114**, 223601 (2015)

Flash Effect

Maryvonne Chalony

Dominique Delande

Romain Pierrat



M. Chalony et al., PRA **84**, 011401(R) (2011)

Romain Pierrat, IL ESPCI (Fr)



Dominique Delande, LKB SU (Fr)



Flash with Λ -Scheme

Chetan S. Madasu

Kwong Chang-Chi

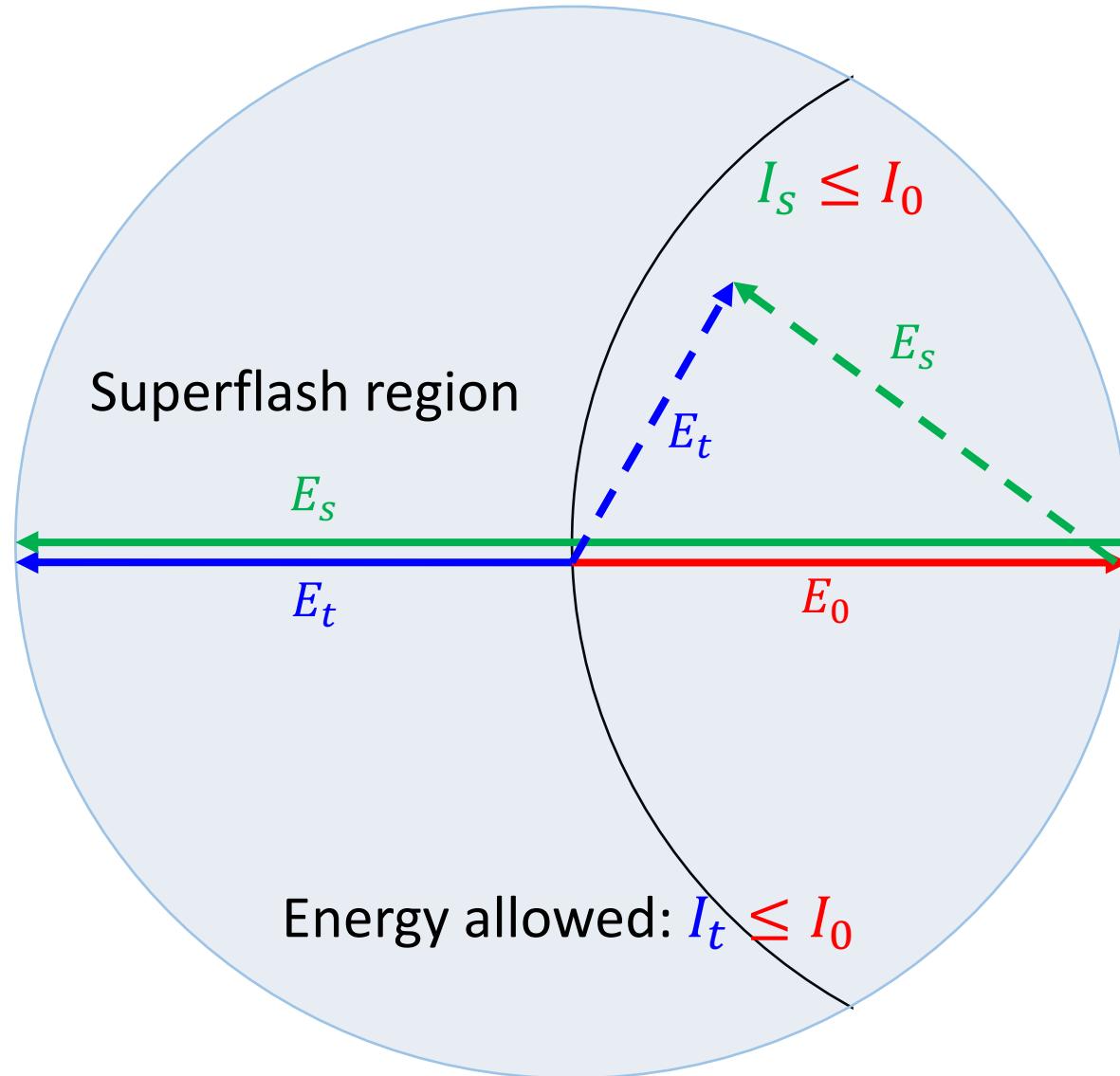
Kanhaiya Pandey



C. Madasu, et al. PRA **105**, 013713 (2022)



Kanhaiya Pandey, IIT Guwahati (In)



$$E_s(\omega) = E_0(\omega) \left[\exp\left(-\frac{b}{2} + i\phi\right) - 1 \right]$$

Max. value: $\exp\left(-\frac{b}{2} + i\phi\right) \rightarrow -1$

So we need: $b \rightarrow 0$ and $\phi \rightarrow \pm\pi$

$$b = \text{Im}\{\alpha\}\rho k L \quad \phi = \frac{\text{Re}\{\alpha\}}{2} \rho k L$$

